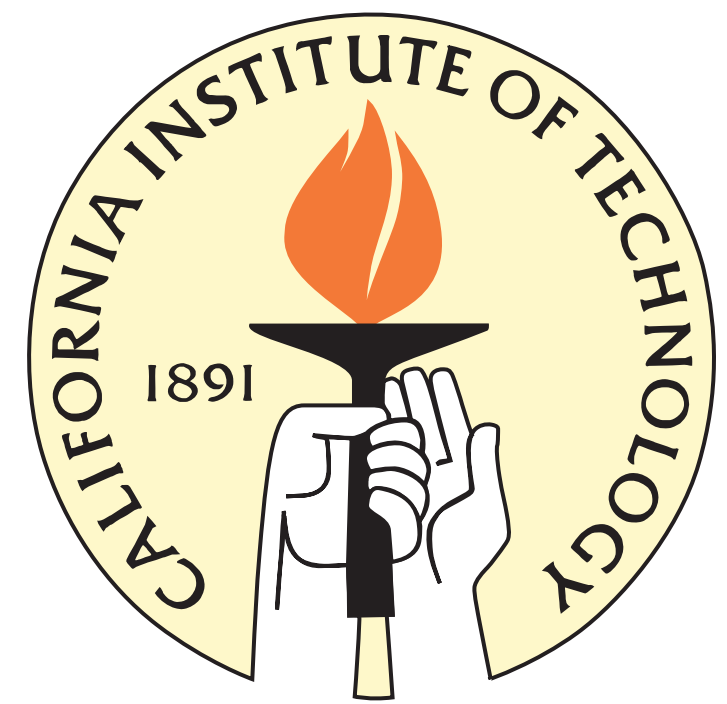


Assimilation of Plate Tectonic Reconstructions into Geodynamic Flow Models



Mark Turner, Mike Gurnis, Lydia Taylor, Vlad Manea, Sonja Kisin
Caltech, Tectonics Observatory

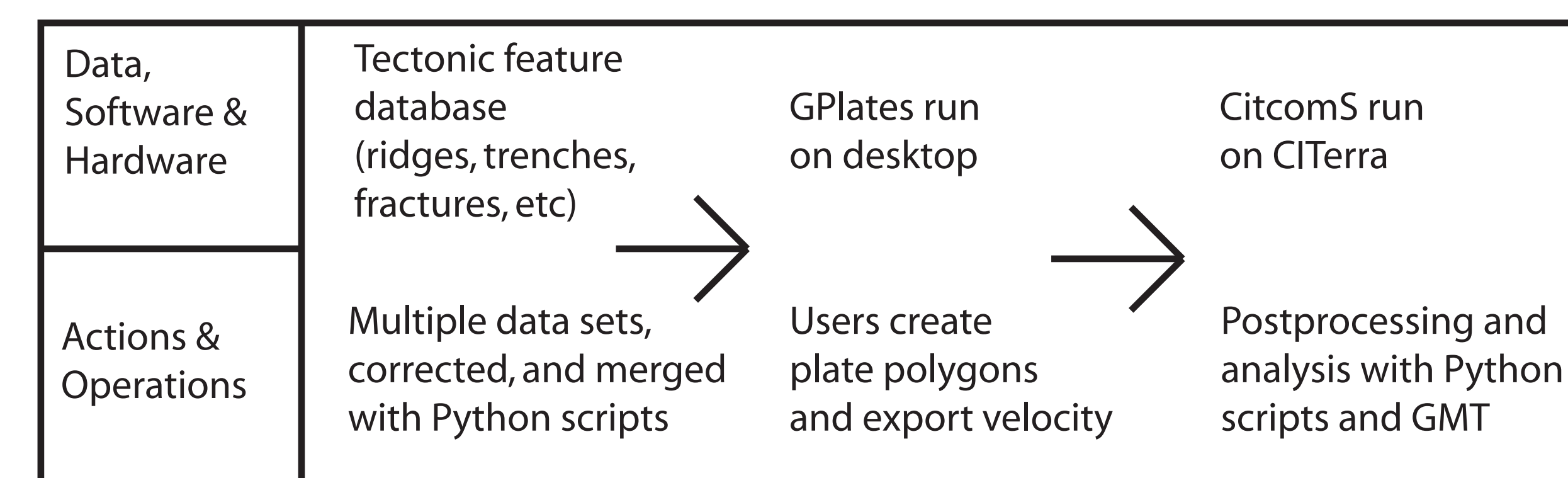
Dietmar Muller, Maria Sdrolia
University of Sydney, School of Geosciences

Introduction

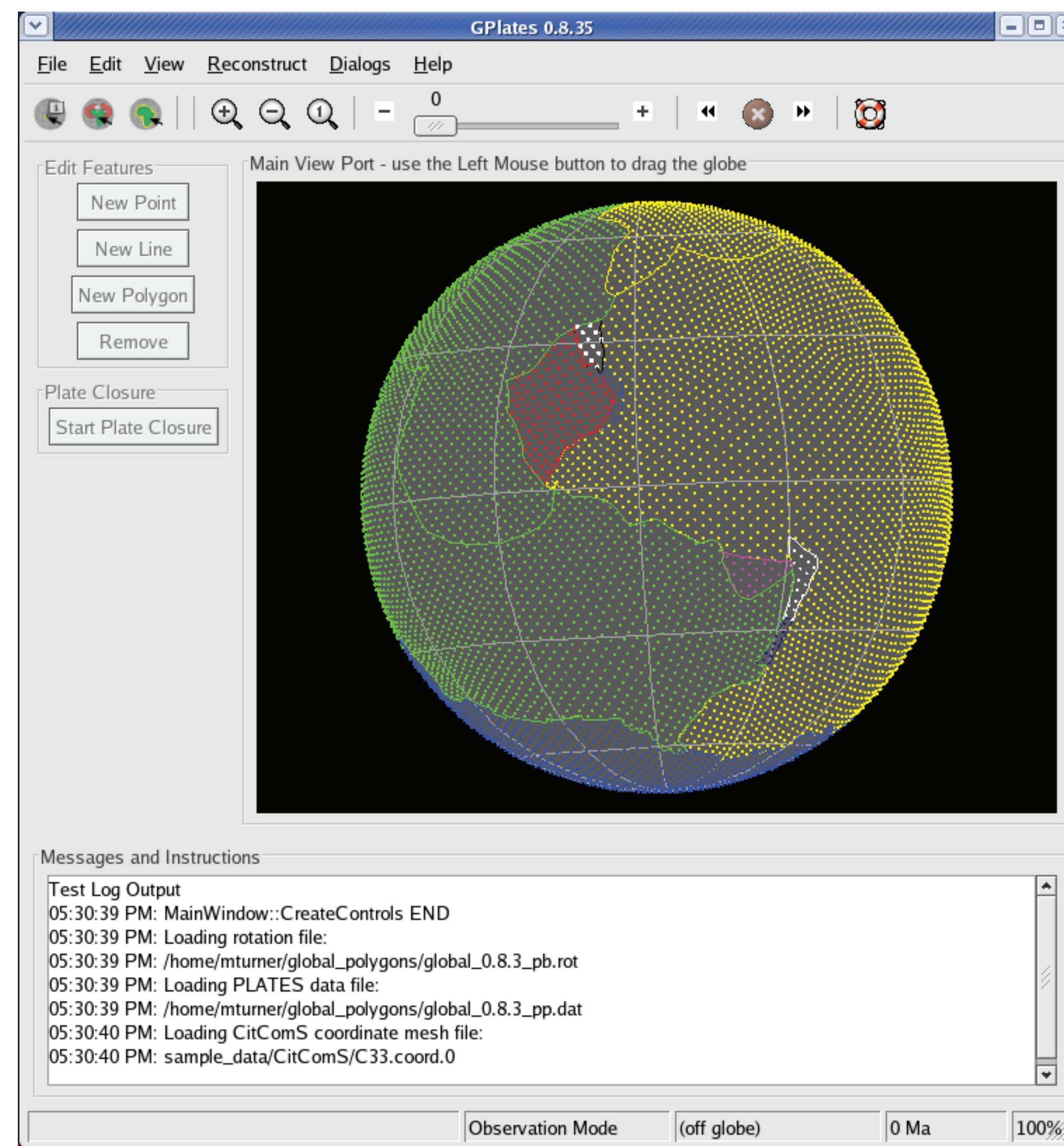
One of our goals is to attempt to place the tectonics of individual boundaries within a global context and to understand the broader scale forces driving the deformation. There are a host of unsolved questions surrounding the causes for changes in plate motions, including the initiation of new subduction zones. In order to address this question, the CTO has been developing an entirely new generation of tools that are computationally advanced while being consistent with the actual structure and kinematics of plate boundaries. Thus far, we have made considerable progress in this direction. One goal is to assimilate plate tectonic reconstructions into global and regional geodynamic models. With the University of Sydney in Australia and the Geological Survey of Norway, the TO has been a key partner in the development of GPlates, a plate tectonic reconstruction software package. We are using GPlates as the preprocessing front end to global models of mantle convection using the CitcomS finite element code.

Using GPlates, we have developed a method for representing the evolving geometry of tectonic plates. A single plate is represented by all of the margins around the plate, reconstructed according to the Euler pole of the margin, and an algorithm for computing the intersections of all of the margins. The end result is a complete evolving description of the surface of the earth without any blank spaces – an essential prerequisite for merging dynamic models with paleo-reconstructions. We have used this software to build a global set of plates over the last 80 million years, to merge these "dynamic" plate polygons with paleo age grids, and to assimilate this data into global circulation models of the mantle. This work has given the CTO a new tool that allows us to explore the dynamics of changes in plate motions and shapes over the next several years. We are now routinely running this software on the CitTerra supercomputer.

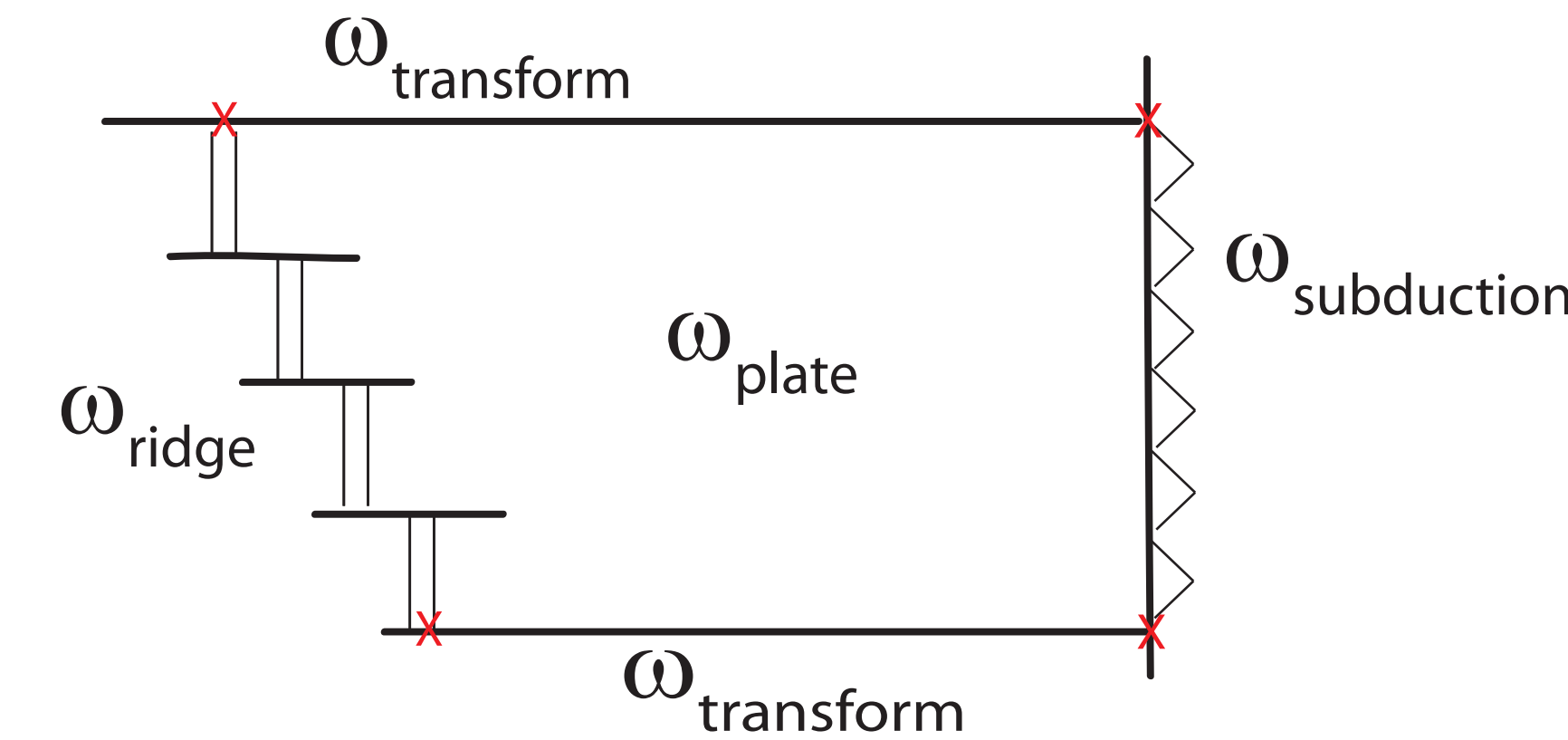
Typical Workflow Assimilating Data into Models



GPlates: Software for Tectonic Reconstructions



An idealized tectonic plate showing component margin line data features. Each line feature has its own Euler pole and rotates according to the rules of plate tectonics.



The user selects line features to create a closed plate polygon. GPlates automatically calculates the intersection points (shown as red x's) to form the complete plate polygon boundary.

Upon each reconstruction all lines rotate independently, and GPlates automatically recomputes the new plate boundary to keep the polygon closed and consistent.

The table below shows a typical plate polygon with its component margins: the IndoAustralian plate from the present day back to five million years ago.

Feature	Order	Start	End	Age	Age of	Age of	Type	Color	Color
1	1	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
2	2	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
3	3	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
4	4	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
5	5	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
6	6	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
7	7	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
8	8	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
9	9	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
10	10	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
11	11	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
12	12	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
13	13	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
14	14	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
15	15	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
16	16	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
17	17	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green
18	18	0.00	0.00	0.00	0.00	0.00	Transform	Blue	Blue
19	19	0.00	0.00	0.00	0.00	0.00	Subduction	Red	Red
20	20	0.00	0.00	0.00	0.00	0.00	Ridge	Green	Green

The GPlates main window has a central globe for display, controls for creation and editing of tectonic feature data, and tools for performing reconstructions and animations. Most feature data may be exported as simple GMT xy files. When combined with a CitcomS mesh, GPlates can export surface velocity vectors for each mesh point.

CitcomS: Mantle Convection Models

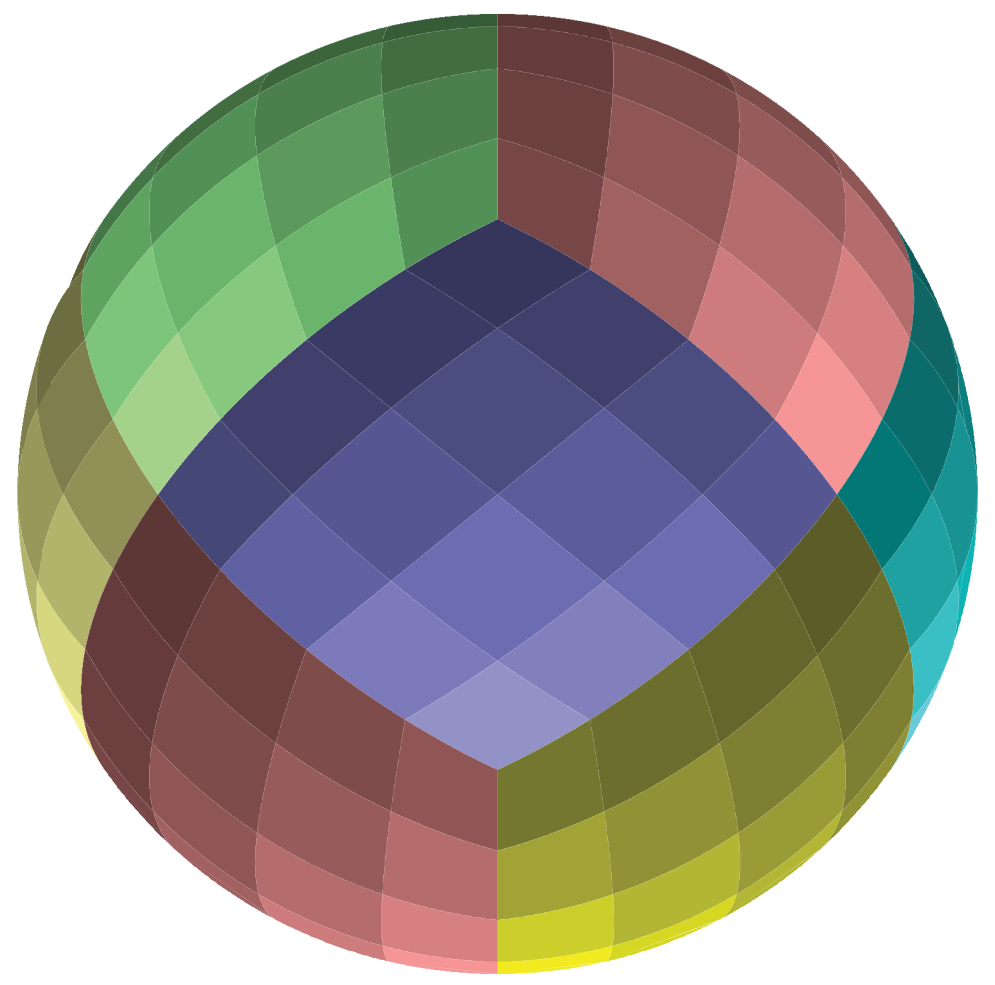
The plate tectonic reconstructions are assimilated into models of mantle convection solved with the finite element package CitcomS.py, developed at Caltech. CitcomS solves for conservation of mass, momentum and energy:

$$\begin{aligned}
 (1) \quad & \nabla \cdot \mathbf{u} = 0 \\
 (2) \quad & \nabla \cdot \boldsymbol{\sigma} = \rho_s \alpha (\bar{T} - T_s) \mathbf{g} \\
 (3) \quad & \frac{\partial T}{\partial t} + \mathbf{u} \cdot \nabla T = \kappa \nabla^2 T + H
 \end{aligned}$$

where \mathbf{u} is velocity, $\boldsymbol{\sigma}$ is the stress tensor, P is dynamic pressure, η is dynamic viscosity, T is temperature, κ is thermal diffusivity, H internal heat and \mathbf{g} is the gravitational acceleration.

These equations are solved with CitcomS.py [Tan et al., 2006] with the finite element. The model domain is a spherical shell representing the entire mantle and lithosphere. CitcomS.py uses a decomposition scheme such that the spherical shell is first decomposed into 12 caps so that in map view the elements are approximately equal area over the entire surface of the sphere. Then each cap is further divided such that the edges of the cap are equally divided.

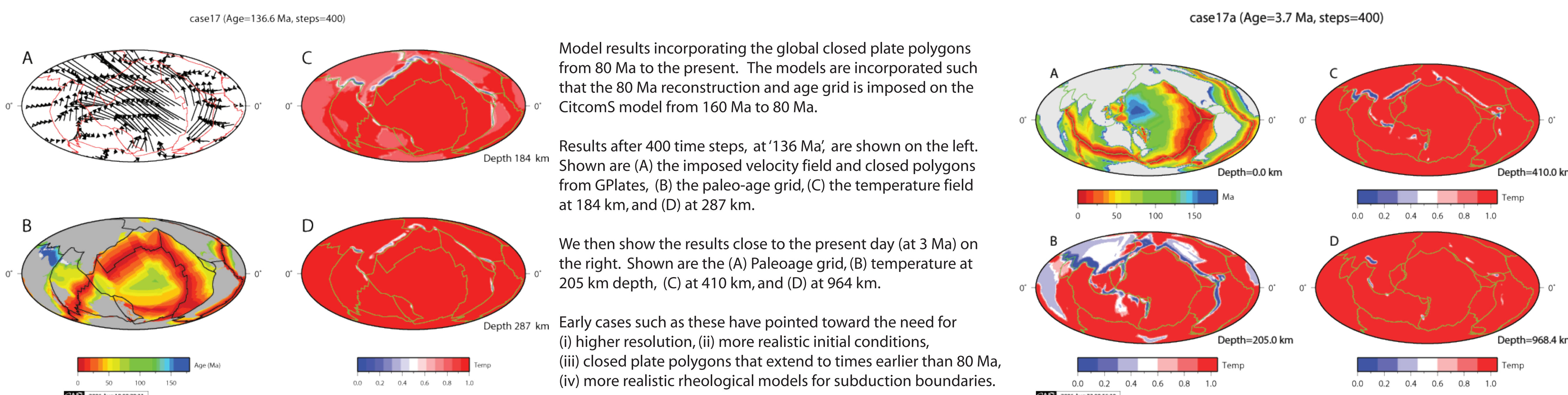
Orthographic projection of processors from a full CitcomS mesh in which there are 16 processors in map view for each cap. The CitcomS cap is shown as distinct colors while the processor domains within the caps are indicated by the intensity of the color.



This example was produced for a run with 2 processors in radius such that the total number of processors was $12 \times 16 \times 2 = 384$. This is the largest model we have solved for on the CitTerra machine so far, and most of the cases have been solved with 96 processors with 128×128 elements in map view for each processor.

References:
Tan, E., E. Choi, P. Thoutireddy, M. Gurnis, and M. Aivazis, GeoFramework: Coupling multiple models of mantle convection within a computational framework, *Geochemistry, Geophysics, Geosystems*, 7, Q06001, doi:10.1029/2005GC001155, 14 pp., 2006.

Global Models with Polygons, Age Grids, and Convection



Assimilation of Age Grids

We have been developing a new method by which the paleo age grids are assimilated into the flow models. We have explored a method by a thermal model for the conductive cooling of the oceanic lithosphere (a half-space model), is used

$$T_e(z, \tau) = T_s + (T_m - T_s) \operatorname{erf}\left(\frac{z}{2\sqrt{\kappa\tau}}\right)$$

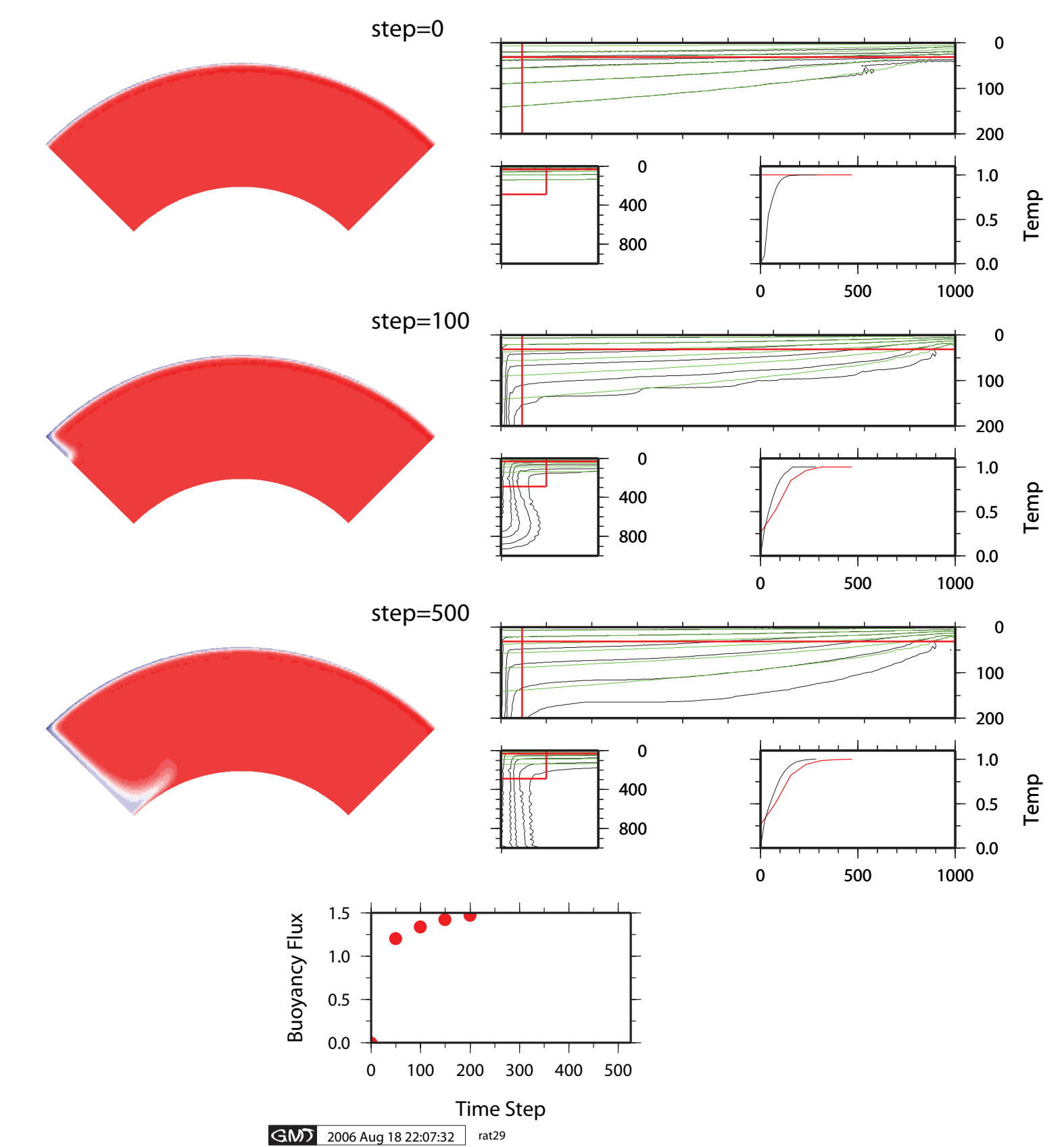
where T_e is the expected temperature, T_s is the surface temperature, T_m is the mantle temperature, z is depth, κ is the thermal diffusivity, and τ is the age of the oceanic lithosphere from the age grid. We attempt to conform the thermal structure within CitcomS to this thermal model for depths less than d_a , the assimilation depth. At each new time-step

$$\gamma = \frac{z}{2d_a} \quad \text{if } z < d_a$$

$T(z, t) = (1 - \gamma)T'(z, t) + \gamma T_e(z, \tau)$ where γ is the depth-dependent assimilation factor and T' is the temperature after the temperature is updated in the normal way by the solution of the energy equation.

In the figure on the right we show how this depth-dependent assimilation affects a simple model of cellular convection using the same set of parameters that we used in the global models, i.e. same Rayleigh number, d_a , age distribution, and resolution. What we find is that if d_a is too close to the thickness of the oceanic lithosphere for a given age, τ , then subduction is cut-off.

On the left is the temperature field for the entire model domain, while on the right we zoom in on the upper thermal boundary layer for three time steps, including the initial condition. In the contour plots on the right, we see the expected temperature contoured in green and the temperatures from CitcomS using $d_a = 0.005$ (32 km).



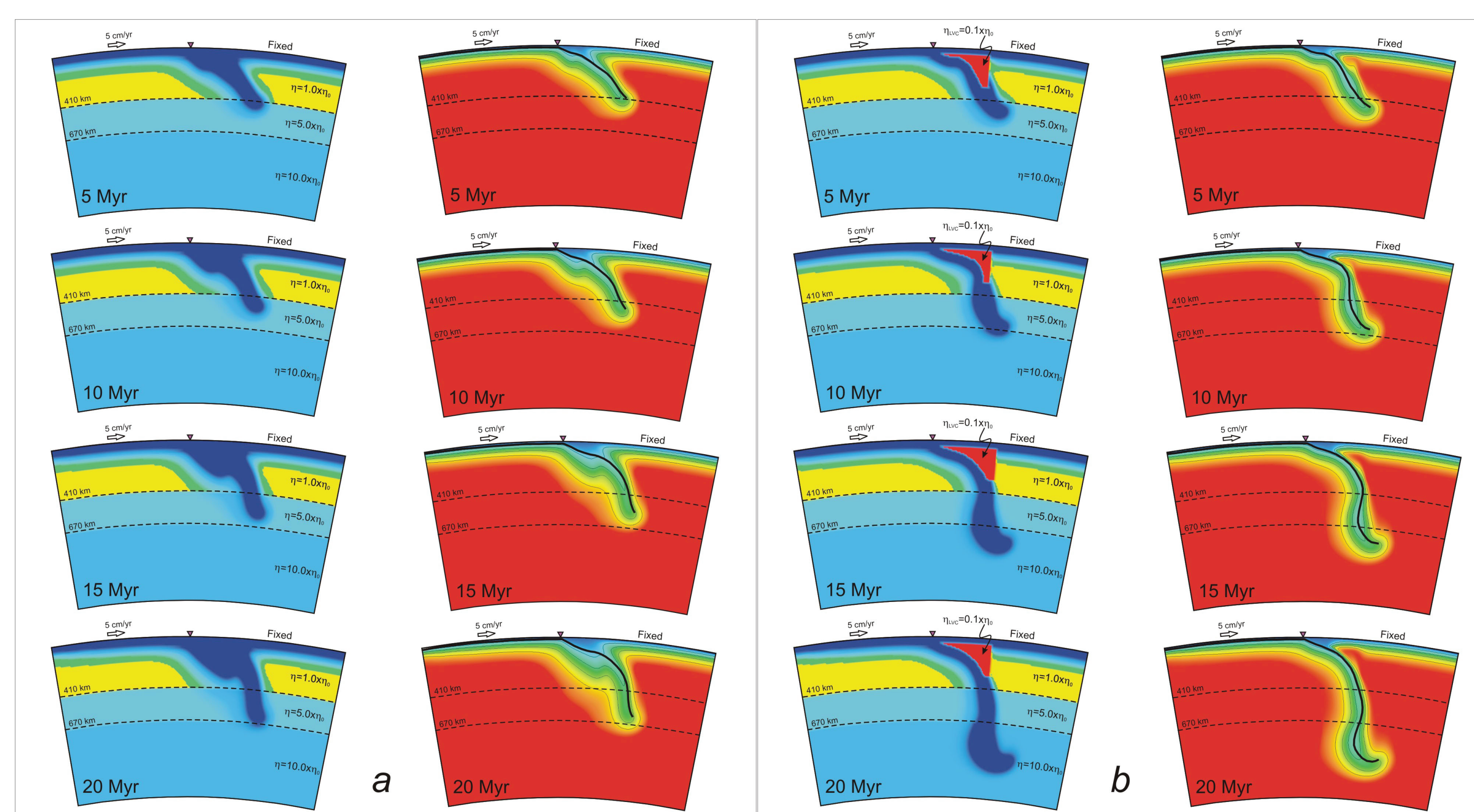
Low Viscosity Wedges

The details of plate margins, especially the introduction of low viscosity wedges (LVWs), can have a substantial influence on the dynamics of subduction zones.

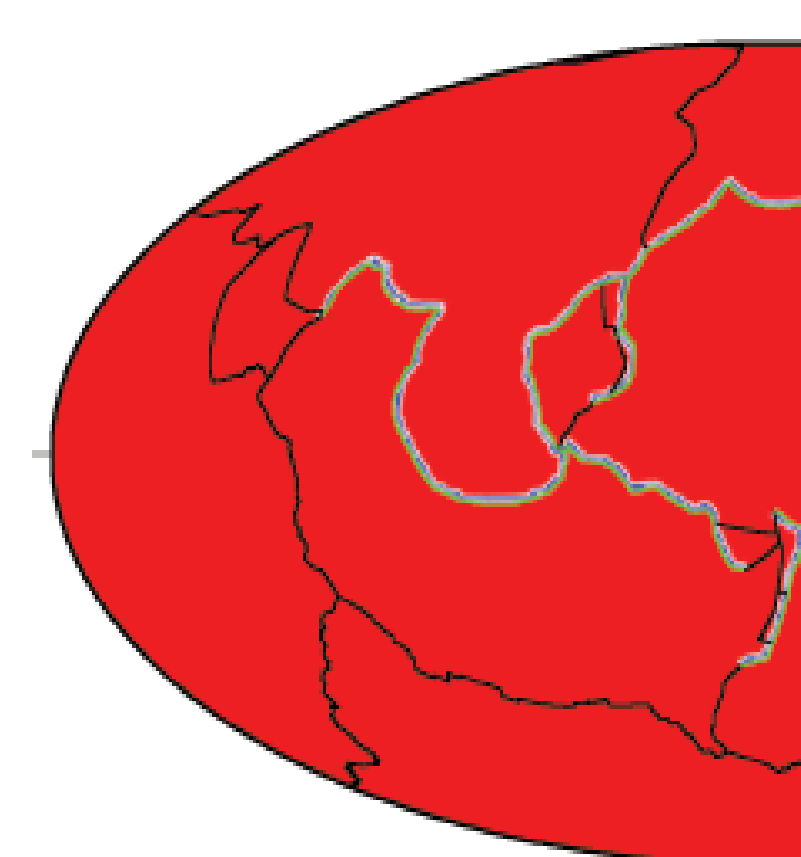
These models show a method we have developed to simulate the weakening of mantle wedge by way of the dehydration of subducted oceanic crust. It relies on tracking the oceanic crust after it has been subducted by way of tracers and then lowering the viscosity of the mantle above the crust in terms of pressure and distance from the trench. The method has been incorporated into the regional version of CitcomS. The models shown are effectively 2-D but the method works in 3-D as well.

In the figures at right, the oceanic crust is shown in Blue on top of the temperature field. In the case shown in (a) there is no mantle wedge and the oceanic lithosphere has been advectively thickened below the over-riding plate.

The only difference in the model shown in (b) is the incorporation of a LVW such that the viscosity between a depth of about 40 km and 300 km has had its viscosity reduced by one order of magnitude. The excessive advective thickening has vanished, the slab dips at a steeper dip into the mantle, and the slab penetrates to a greater depth into the mantle for an equal interval of time.



Incorporation of Asymmetric Plate Boundaries from GPlates into CitcomS



We have been able to complete the workflow from subduction zones, including their polarity from the plate tectonic reconstruction (GPlates) and merged with CitcomS (shown at left). We are currently refining the procedure.

Shown at left is an image of the material type before incorporation into CitcomS as a raster image from red (normal) to blue (weak plate boundaries). GPlates distinguishes between the closed plate polygon (black lines) and the subduction boundaries (green lines).

These material types are then processed by CitcomS with the other controls on the viscosity (pressure and temperature) to create the viscosity shown at right, with the three cross-sections with the low viscosity wedges shown as the deepest red.

