

# Analysis of long-period seismic waves excited by the 2012 Off-Sumatra earthquake

Zacharie Duputel, Victor Tsai, Hiroo Kanamori, Luis Rivera, Lingsen Meng, Jean-Paul Ampuero, Joann Stock.

## 1. Abstract

Great strike-slip earthquakes are very uncommon and it is known that many of them involve remarkable rupture complexity. On 11 April 2012, the equatorial Indian Ocean was hit by a  $M_w=8.6$  earthquake, followed two hours later by another  $M_w=8.2$  event. Our analysis for the  $M_w=8.6$  mainshock reveals a remarkable rupture complexity and indicates a large centroid depth ( $\sim 30$ km). To resolve the rupture process, we developed a method to invert long period seismic data for multiple-point-source parameters. The optimum source model at long period consists of two sources with  $M_w=8.5$  and  $M_w=8.3$ . To analyze the  $M_w=8.2$  aftershock, we removed the perturbation due to surface-wave arrivals of the mainshock by subtracting the corresponding synthetics. Our results suggest that the  $M_w=8.2$  aftershock had a large centroid depth between 30 km and 40 km. The large centroid depths observed for the mainshock and the  $M_w=8.2$  aftershock suggest that this sequence most likely breaks the entire oceanic lithosphere thickness. This major earthquake sequence thus brings a new perspective to the seismotectonics of the equatorial Indian Ocean and reveals active deep lithospheric deformations that may ultimately lead to a localized plate boundary.

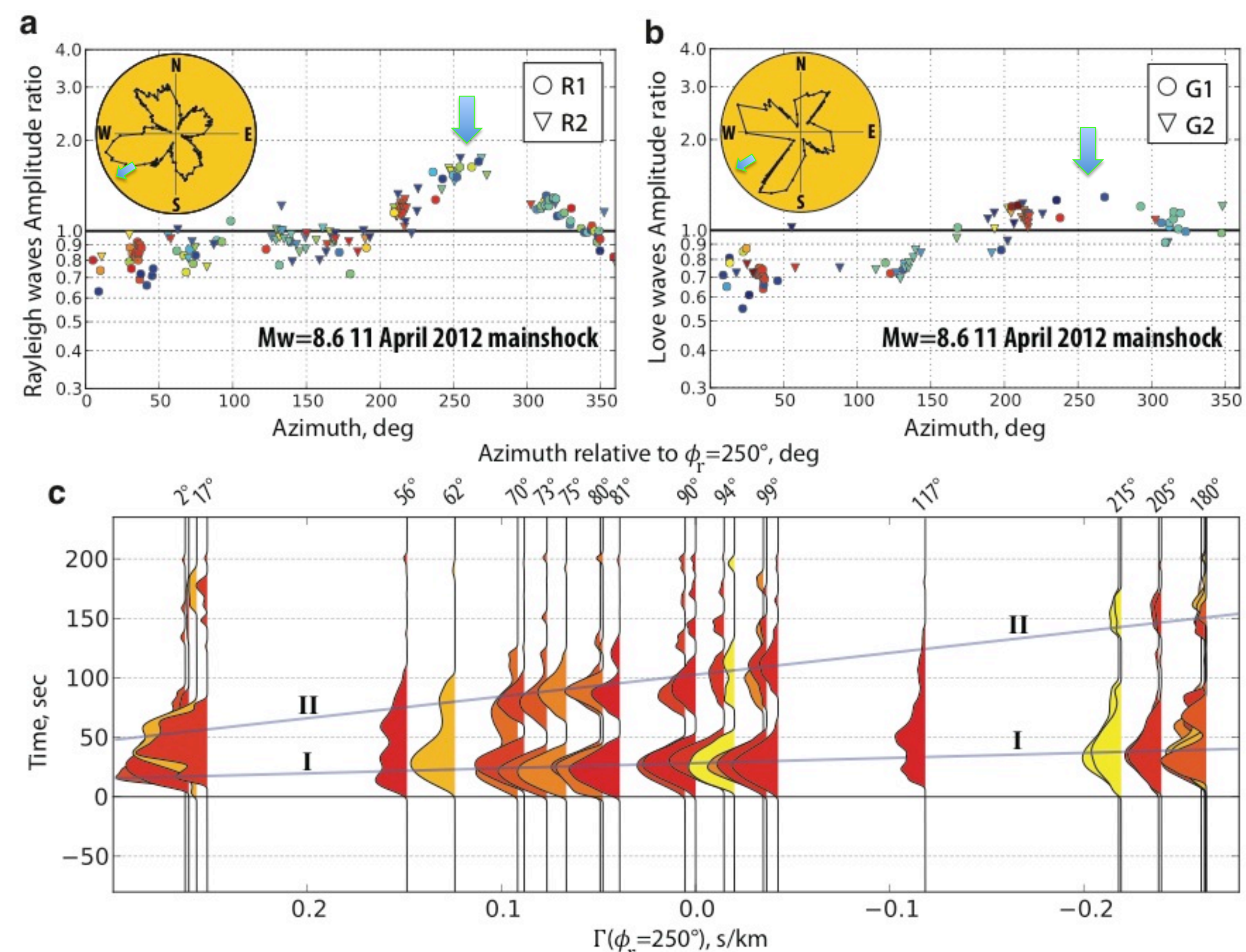
## 2. Methods

**2.1 W-phase Inversion for Point-Source Geometry.** Point-source parameters of  $M_w \geq 5.8$  events during the 2012 Off-Sumatra earthquake sequence are inverted using the W phase algorithm (Fig. 1). The moment tensor components as well as the centroid locations and timings are resolved following the procedure described by Duputel et al. (2012).

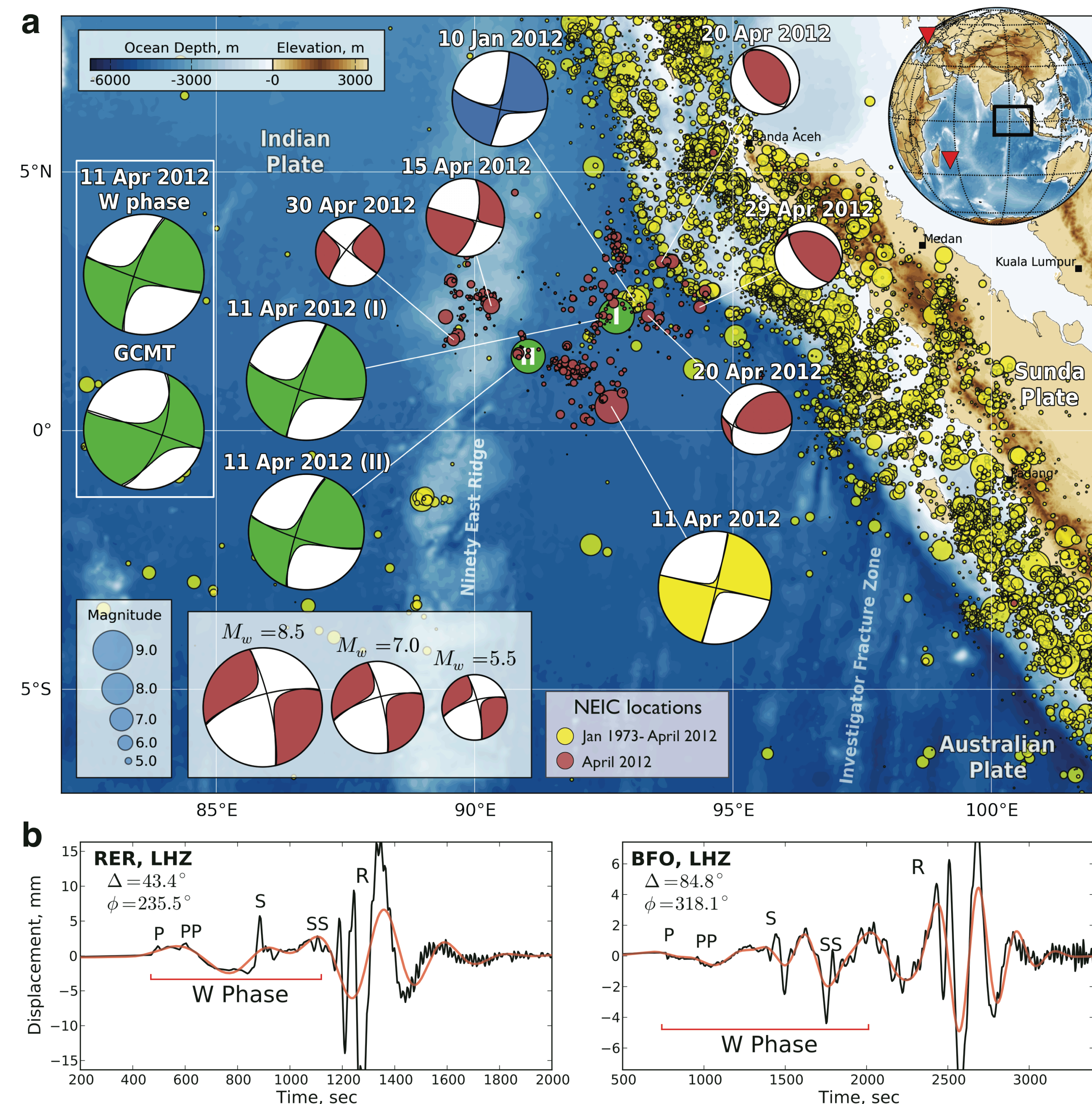
**2.2 Surface-wave directivity and radiation pattern.** To obtain the surface-wave radiation patterns, seismograms  $U(\omega, \Delta, \phi)$  are equalized to  $\Delta_0=90^\circ$  (insets in Fig. 2a-b). To further analyze the directivity, we measure the ratio between observed amplitude and predicted surface-wave amplitudes for a point-source in the 200-400 s passband (Fig. 2a-b).

**2.3 Surface-wave moment rate functions.** We compute broadband (25s-600s) R1 Rayleigh-wave moment rate functions by deconvolving point-source synthetics from data (Fig. 2c). The deconvolution is performed using the projected Landweber method imposing causality and positivity. We use SEM synthetics for a 3D Earth model (S362ANI and Crust2.0).

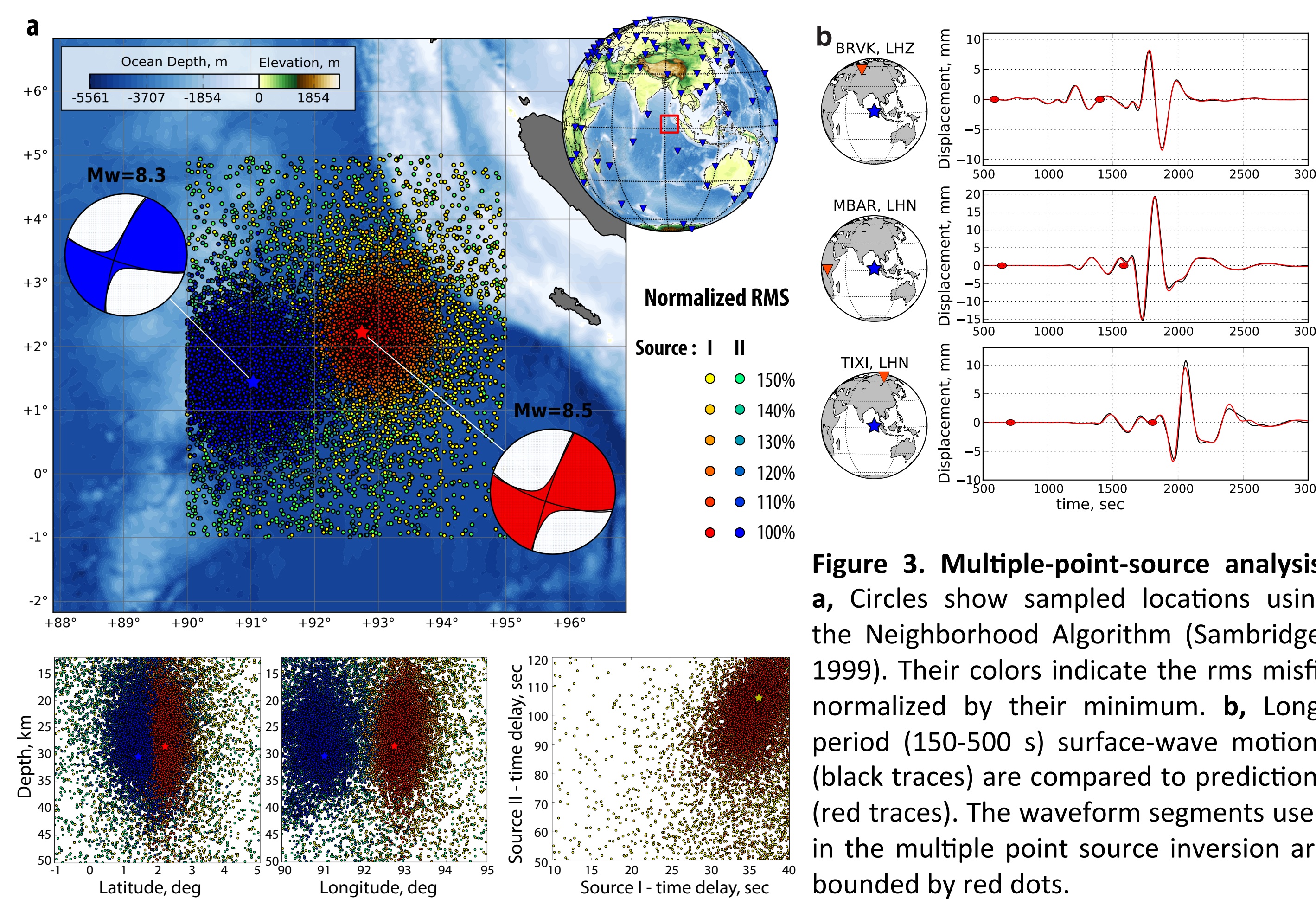
**2.4 Multiple point source analysis.** To account for the MRFs suggesting at least two distinct subevents for the mainshock, we perform a two-point-source inversion (Fig. 1 and Fig. 3). We invert for the subevent moment tensors, locations (latitudes, longitudes, depths), time delays and half durations using a modified version of the Neighborhood Algorithm sampler.



**Figure 2. Long period Surface-wave analysis for the  $M_w=8.6$  mainshock.** Obs./Pred. ratios are presented for **a**, Rayleigh waves and **b**, Love waves. The Inset diagrams are equalized Rayleigh and Love waves. **c**, R1 Rayleigh wave Moment Rate Functions (MRFs) ordered as a function of the directivity parameter  $\Gamma = \cos(\phi - \phi_0)/c$ , assuming  $\phi_0 = 250^\circ$  and  $c=3.8$ km/s. Amplitude ratios and R1 MRFs are colored as a function of the epicentral distance ( $\Delta$ ).

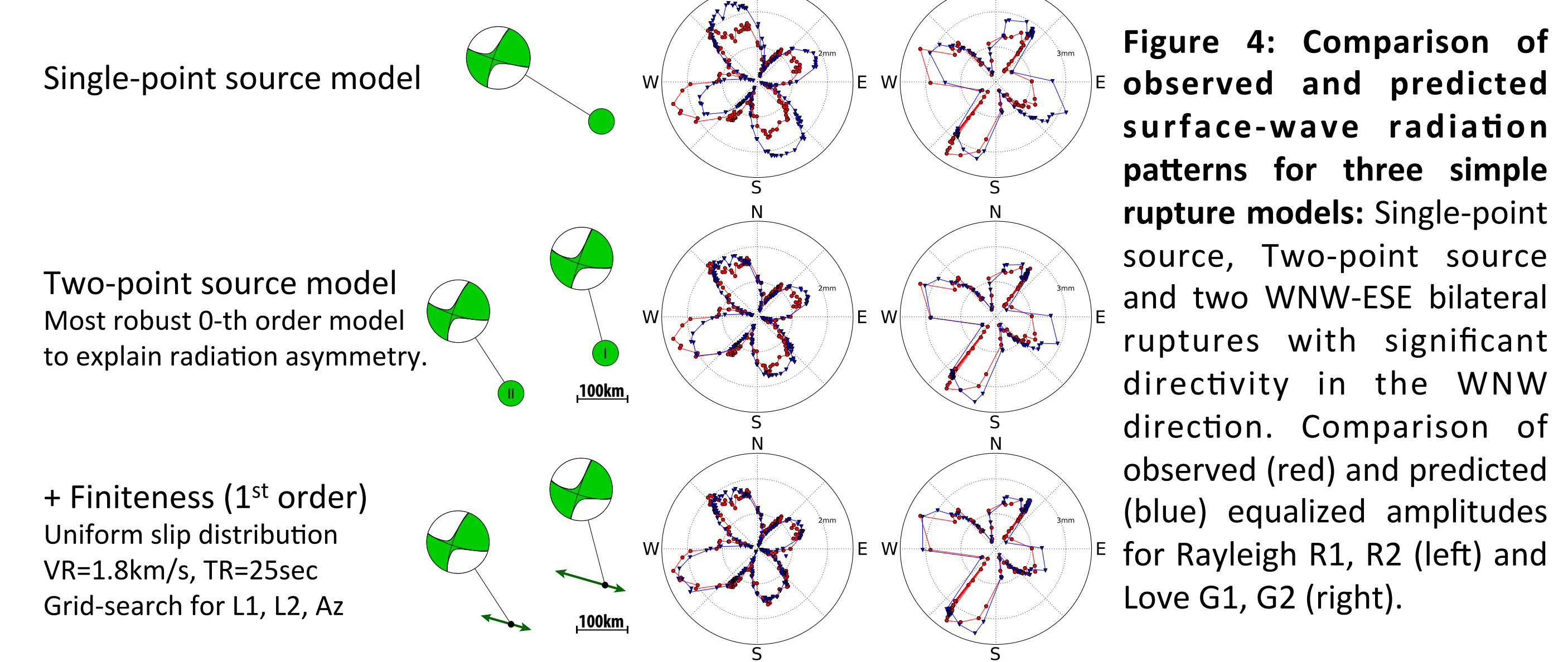


**Figure 1. The 2012 Sumatra great earthquake sequence.** **a**, Off-Sumatra earthquake region. The  $M_w=8.6$  mainshock can be decomposed in two subevents (green mechanisms and circles labeled I and II). The W phase and Global CMT solutions for the mainshock (inset green mechanisms), the W phase solutions for the 10 January foreshock (blue mechanism), for the  $M_w=8.2$  aftershock (yellow) and for the  $5.8 < M_w < 8.2$  aftershocks (red) are shown. **b**, W phase waveforms recorded at station RER and BFO during the mainshock. The black trace is the broad-band data and the red trace is the data filtered in the 200-1000 s passband.



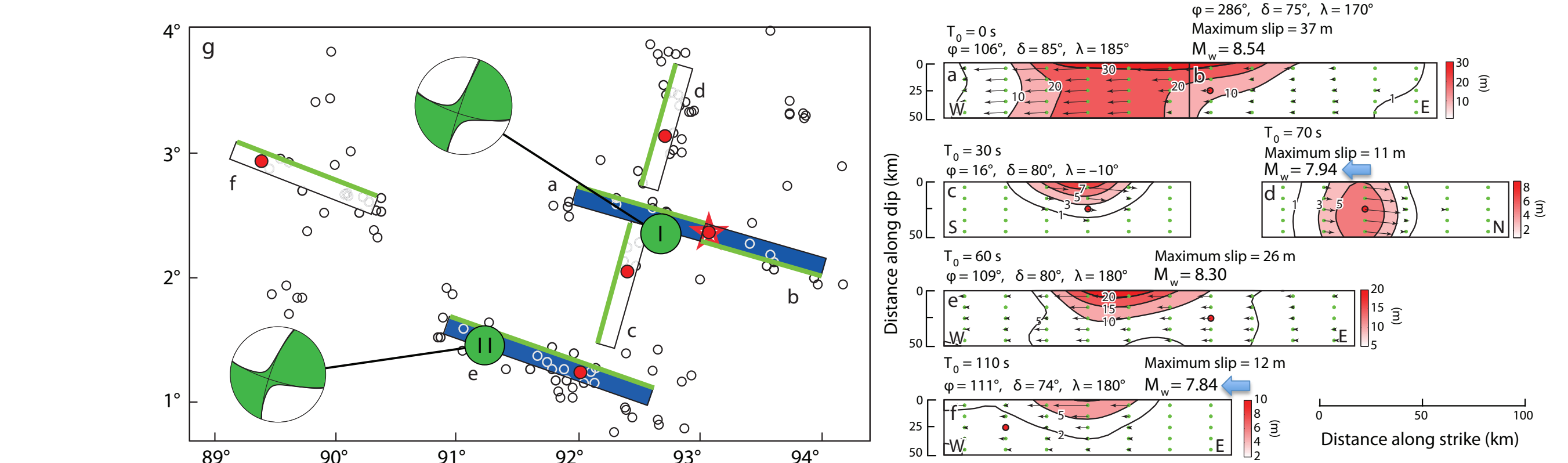
**Figure 3. Multiple-point-source analysis.** **a**, Circles show sampled locations using the Neighborhood Algorithm (Sambridge, 1999). Their colors indicate the rms misfit normalized by their minimum. **b**, Long-period (150-500 s) surface-wave motions (black traces) are compared to predictions (red traces). The waveform segments used in the multiple point source inversion are bounded by red dots.

## 3. First order directivity analysis



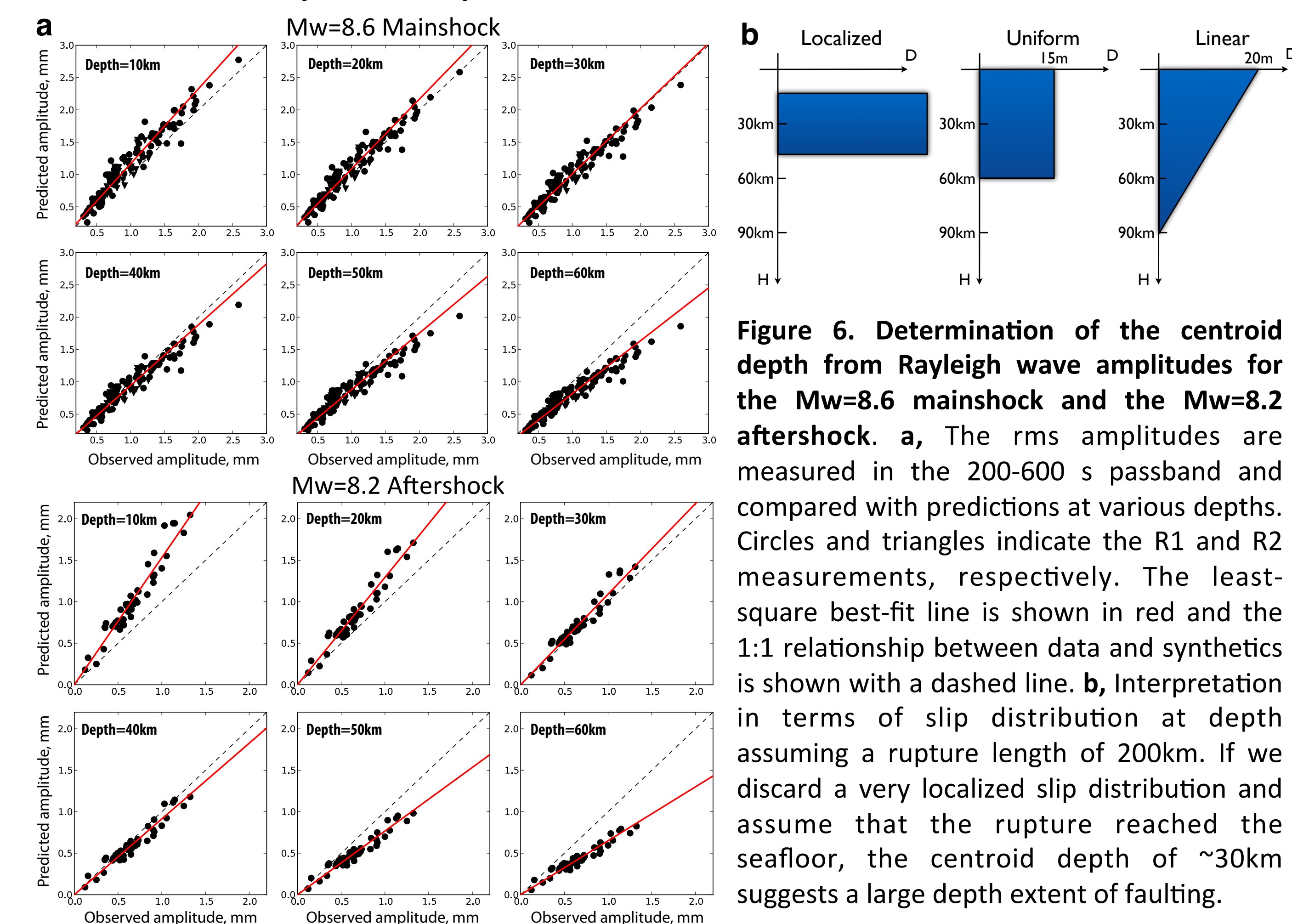
**Figure 4: Comparison of observed and predicted surface-wave radiation patterns for three simple rupture models:** Single-point source, Two-point source and two WNW-ESE bilateral ruptures with significant directivity in the WNW direction. Comparison of observed (red) and predicted (blue) equalized amplitudes for Rayleigh R1, R2 (left) and Love G1, G2 (right).

## 4. Comparison with preliminary finite-fault modeling



**Figure 5. Comparison with the slip distribution model proposed by Yue et al. (2012).** There is a dominant contribution from WNW-ESE faults, consistent with the first order directivity analysis.

## 5. Evidence of complete lithospheric failure



**Figure 6. Determination of the centroid depth from Rayleigh wave amplitudes for the  $M_w=8.6$  mainshock and the  $M_w=8.2$  aftershock.** **a**, The rms amplitudes are measured in the 200-600 s passband and compared with predictions at various depths. Circles and triangles indicate the R1 and R2 measurements, respectively. The least-square best-fit line is shown in red and the 1:1 relationship between data and synthetics is shown with a dashed line. **b**, Interpretation in terms of slip distribution at depth assuming a rupture length of 200km. If we discard a very localized slip distribution and assume that the rupture reached the seafloor, the centroid depth of  $\sim 30$ km suggests a large depth extent of faulting.

## 6. Summary

The  $M_w=8.6$  Sumatra earthquake involved a remarkable rupture complexity. Our analysis of long period seismic waves yielded a simple two point source model and reveals substantial deep lithospheric deformation that may eventually lead to the formation of a localized plate boundary.

## 7. References

- Duputel, Z., Kanamori, H., Tsai, V.C., Rivera, L., Meng, L., Ampuero, J.-P., Stock, J., 2012. Earth Planet Sci. Lett., 351, 247-257.  
 Duputel, Z., Rivera, L., Kanamori, H., Hayes, G., 2012. Geophys. J. Int. 189, 1125-1147.  
 Sambridge, M., 1999. Geophys. J. Int. 138, 479-494.  
 Yue, H., Lay, T., Koper, K.D., 2012. Nature. 490, 245-249.